



ESTABILIDAD I Clase 7

Reticulados - Bastidores

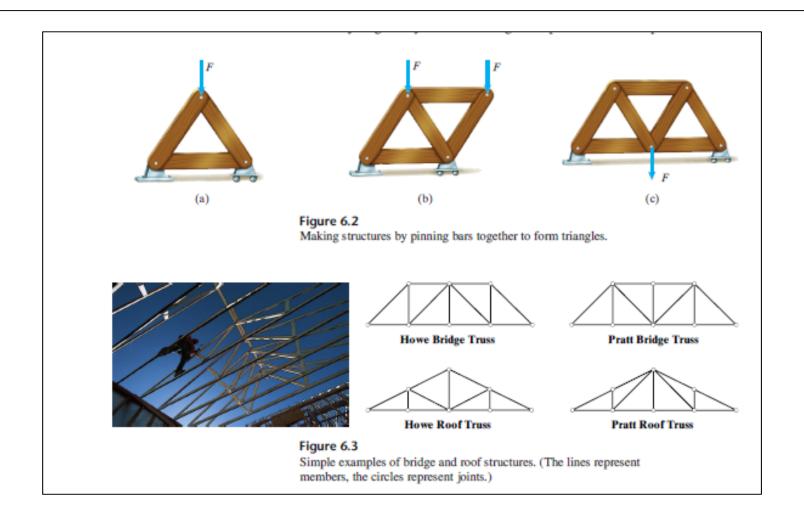
RETICULADOS

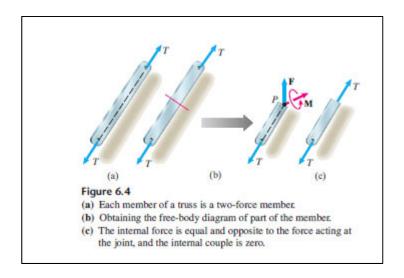


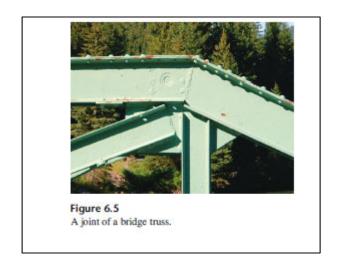


- ➤ **DEFINICIÓN:** Estructuras formada por barras vinculadas entre si en sus extremos, constituyendo un sistema rígido e indeformable.
- ➤ BARRA: Elemento rígido en indeformable con una dimensión predominante respecto de las otras dos.
- ➤ **NUDO:** Punto donde se unen entre si las barras.

Reticulados

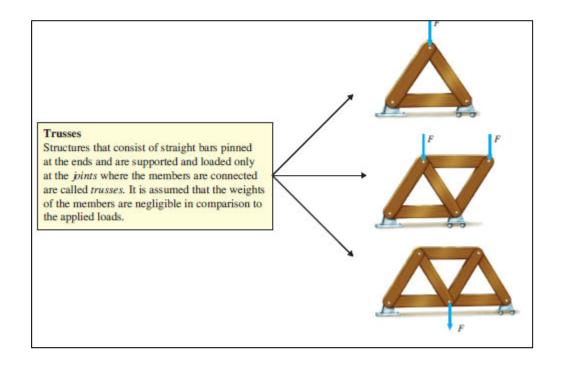






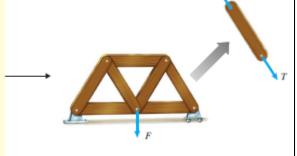
Although many actual structures, including roof trusses and bridge trusses, consist of bars connected at the ends, very few have pinned joints.

For example, a joint of a bridge truss is shown in Fig. 6.5. The ends of the members are welded at the joint and are not free to rotate. It is obvious that such a joint can exert couples on the members. Why are these structures called trusses? The reason is that they are designed to function as trusses, meaning that they support loads primarily by subjecting their members to axial forces. They can usually be *modeled* as trusses, treating the joints as pinned connections under the assumption that couples they exert on the members are small in comparison to axial forces. When we refer to structures with riveted joints as trusses in problems, we mean that you can model them as trusses.



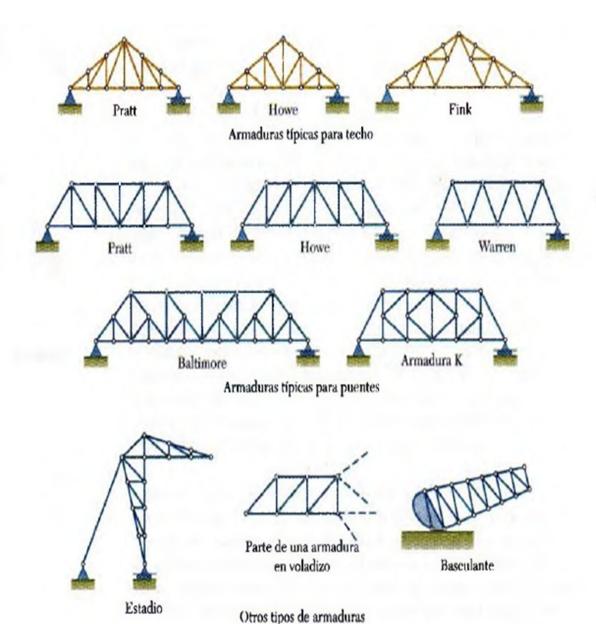
Free-Body Diagram of an Individual Member

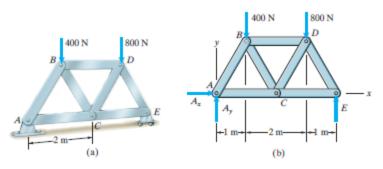
Because each member of a truss is a two-force member, it is subjected only to equal and opposite axial loads. We call the force T the axial force in a member. When T is positive in the direction shown (that is, when the forces are directed away from each other), the member is in tension (T). When the forces are directed toward each other, the member is in compression (C).

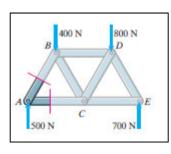


DISTINTOS TIPOS DE RETICULADOS PLANOS



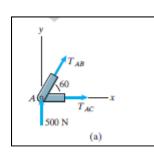


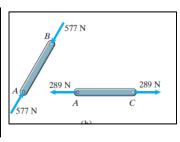


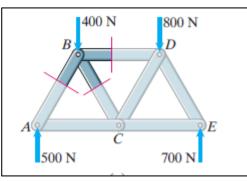


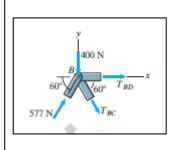
$$\Sigma F_x = A_x = 0,$$

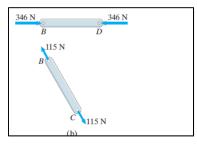
 $\Sigma F_y = A_y + E - 400 \text{ N} - 800 \text{ N} = 0,$
 $\Sigma M_{\text{point }A} = -(1 \text{ m})(400 \text{ N}) - (3 \text{ m})(800 \text{ N}) + (4 \text{ m})E = 0,$
e obtain the reactions $A_x = 0$, $A_y = 500 \text{ N}$, and $E = 700 \text{ N}$.











The equilibrium equations for joint A are

$$\Sigma F_x = T_{AC} + T_{AB} \cos 60^\circ = 0,$$

 $\Sigma F_v = T_{AB} \sin 60^\circ + 500 \text{ N} = 0.$

Solving these equations, we obtain the axial forces
$$T_{AB} = -577 \text{ N}$$
 and $T_{AC} = 289 \text{ N}$. Member AB is in compression, and member AC is in tension

We next obtain a free-body diagram of joint B by cutting members AB, BC, and BD (Fig. 6.8a). From the equilibrium equations for joint B,

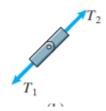
$$\Sigma F_x = T_{BD} + T_{BC} \cos 60^\circ + 577 \cos 60^\circ \text{N} = 0,$$

 $\Sigma F_y = -400 \text{ N} + 577 \sin 60^\circ \text{N} - T_{BC} \sin 60^\circ = 0,$

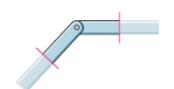
we obtain $T_{BC} = 115$ N and $T_{BD} = -346$ N. Member BC is in tension, and member BD is in compression (Fig. 6.8b). By continuing to draw free-body diagrams of the joints, we can determine the axial forces in all of the members.

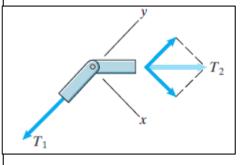
- Truss joints with two collinear members and no load (Fig. 6.9). The sum of the forces must equal zero, $T_1 = T_2$. The axial forces are equal.
- Truss joints with two noncollinear members and no load (Fig. 6.10). Because the sum of the forces in the x direction must equal zero, $T_2 = 0$. Therefore T_1 must also equal zero. The axial forces are zero.
- Truss joints with three members, two of which are collinear, and no load (Fig. 6.11). Because the sum of the forces in the x direction must equal zero, $T_3 = 0$. The sum of the forces in the y direction must equal zero, so $T_1 = T_2$. The axial forces in the collinear members are equal, and the axial force in the third member is zero.

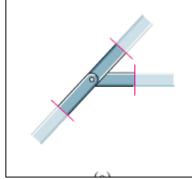


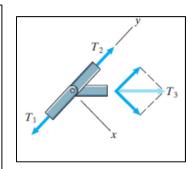


- (a) A joint with two collinear members and no load.
- (b) Free-body diagram of the joint.



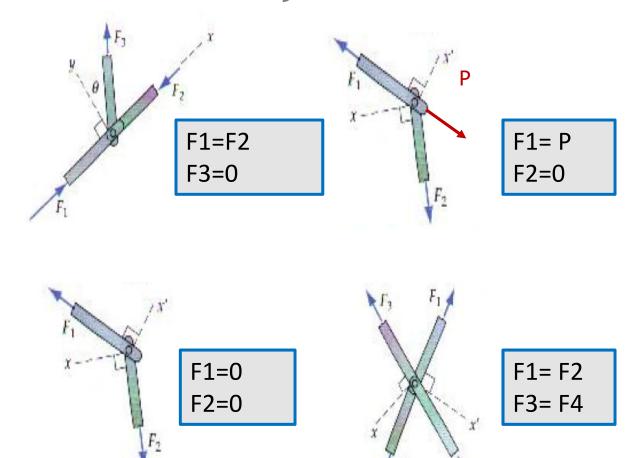


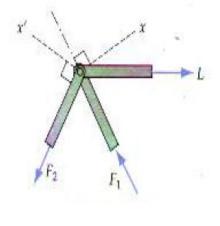






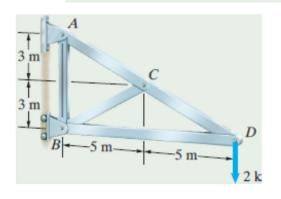
BARRAS INACTIVAS y CASOS PARTICULARES

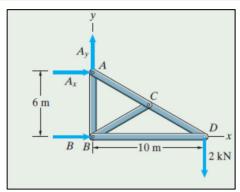




ELECCIÓN DE EJES
CONVENIENTES,
OBTENCIÓN DE UN
SISTEMA DE
ECUACIONES
DESACOPLADAS

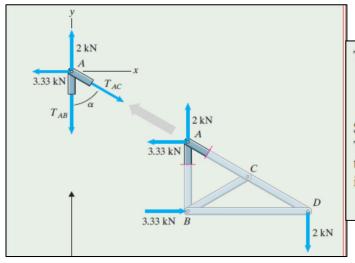
Determine the axial forces in members AB and AC of the truss.





$$\Sigma F_x = A_x + B = 0,$$

 $\Sigma F_y = A_y - 2 \text{ kN} = 0,$
 $\Sigma M_{\text{point } B} = -(6 \text{ m}) A_x - (10 \text{ m})(2 \text{ kN}) = 0.$
Solving yields $A_x = -3.33 \text{ kN}, A_y = 2 \text{ kN},$
and $B = 3.33 \text{ kN}.$



The angle $\alpha = \arctan(5/3) = 59.0^{\circ}$.

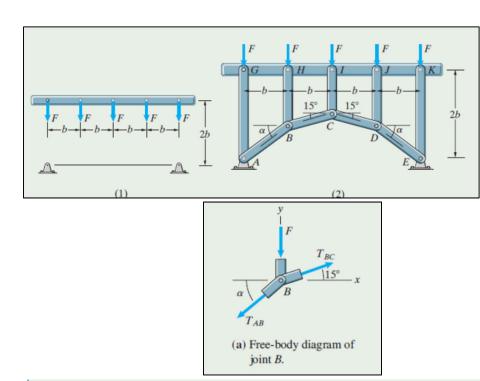
$$\Sigma F_x = T_{AC} \sin \alpha - 3.33 \text{ kN} = 0,$$

$$\Sigma F_{v} = 2 \text{ kN} - T_{AB} - T_{AC} \cos \alpha = 0.$$

Solving yields $T_{AB} = 0$ and $T_{AC} = 3.89$ kN. The axial force in member AB is zero and the axial force in member AC is 3.89 kN in tension, which we write as

AB: zero, AC: 3.89 kN (T).

The loads a bridge structure must support and pin supports where the structure is to be attached are shown in Fig. 1. Assigned to design the structure, a civil engineering student proposes the structure shown in Fig. 2. What are the axial forces in the members?



Members	Axial Force
AG, BH, CI, DJ, EK	F(C)
AB, DE	2.39F(C)
BC, CD	1.93F(C)

From the equilibrium equations

$$\Sigma F_x = -T_{AB}\cos\alpha + T_{BC}\cos 15^\circ = 0,$$

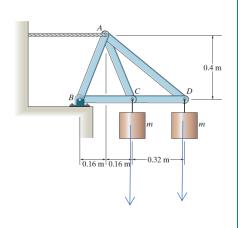
$$\Sigma F_{y} = -T_{AB}\sin\alpha + T_{BC}\sin15^{\circ} - F = 0,$$

we obtain $T_{AB} = -2.39F$ and $\alpha = 38.8^{\circ}$. By symmetry, $T_{DE} = T_{AB}$. The axial forces in the members are shown in the table.



Método de los nudos

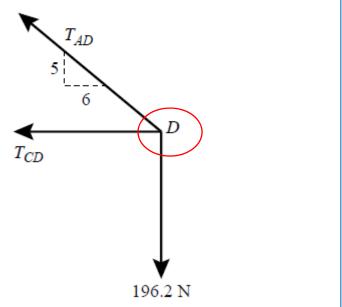
$$m=20 \text{ kg} => P=196.2 \text{ N}$$



$$\sum F_y : \frac{5}{\sqrt{61}} T_{AD} - 196.2 \text{ N} = 0$$

$$\sum F_x : -\frac{6}{\sqrt{61}} T_{AD} - T_{CD} = 0$$

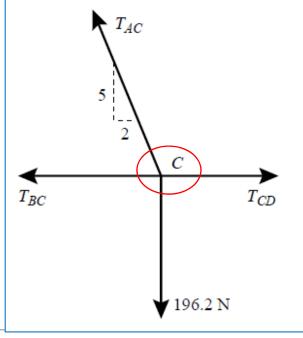
Solving: $T_{AD} = 306 \text{ N}$, $T_{CD} = -235 \text{ N}$



$$\sum F_y : \frac{5}{\sqrt{29}} T_{AC} - 196.2 \text{ N} = 0$$

$$\sum F_x : -\frac{2}{\sqrt{29}} T_{AC} - T_{BC} + T_{CD} = 0$$

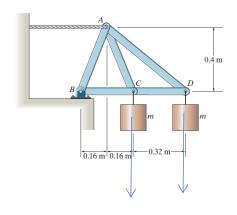
Solving: $T_{AC} = 211 \text{ N}, T_{BC} = -313 \text{ N}$

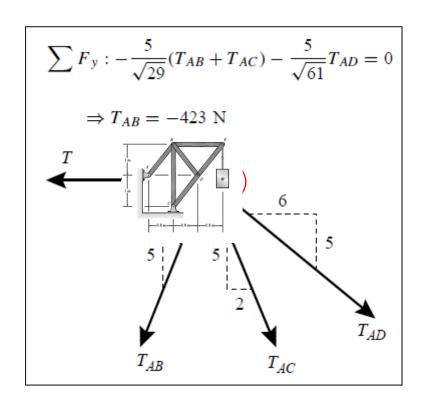




Método de los nudos m=20 kg => P=196.2 N

$$m=20 \text{ kg} => P=196.2 \text{ N}$$





$$T_{AB} = 423 \text{ N}(C)$$

$$T_{AC} = 211 \text{ N}(T)$$

$$T_{AD}=306~{\rm N}(T)$$

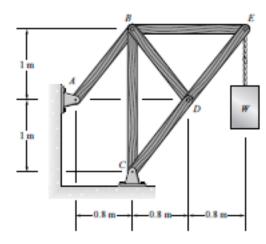
$$T_{BC} = 314 \ \mathrm{N}(C)$$

$$T_{CD} = 235 \text{ N}(C)$$



38.66

Dada la Estructura de la Figura, establezca cual es la maxima carga que soporta si la maxima fuerza en traccion de las barras es 5 kN, y la maxima fuerza en compression es 7 kN



Joint B:

$$\sum F_x = BE - AB\sin\alpha - BD\sin\alpha = 0,$$

from which
$$AB = \frac{BE}{\sin \alpha} = 1.28W(T)$$

$$\sum F_y = -AB\cos\alpha - BC = 0,$$

from which
$$BC = -AB\cos\alpha = -W(C)$$

Joint E:

$$\sum F_{y} = -DE\cos\alpha - W = 0,$$

from which
$$DE = -1.28W$$
 (C)

$$\sum F_y = -BE - DE \sin \alpha = 0,$$

from which
$$BE = 0.8W (T)$$

Joint D:

$$\sum F_x = DE\cos\alpha + BD\cos\alpha - CD\cos\alpha = 0,$$

from which BD - CD = -DE.

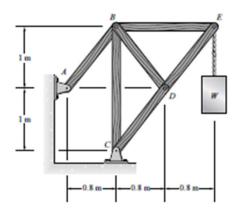
$$\sum F_y = -BD\sin\alpha + DE\sin\alpha - CD\sin\alpha = 0,$$

from which BD + CD = DE.

Solving these two equations in two unknowns:

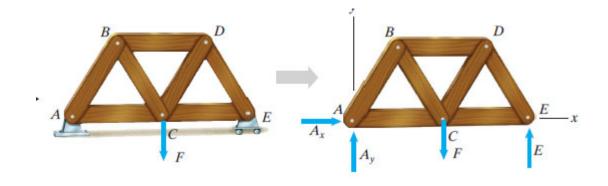
$$CD = DE = -1.28W (C), BD = 0$$

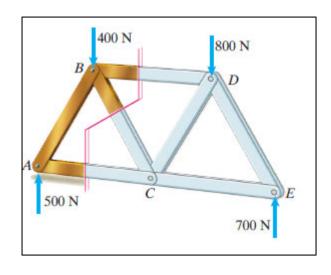


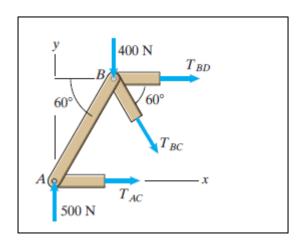


				F admisible	W max
AB	1.28 W	Т	1.28	5	3.90625
BC	W	C	-1		
CD	1.28W	С	-1.28		
DE	1.28W	С	-1.28	-7	5.46875
BE	0.8 W	Т	0.8		

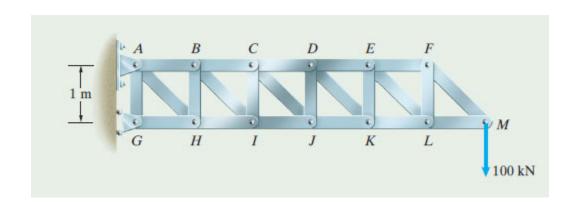
Método de las Secciones

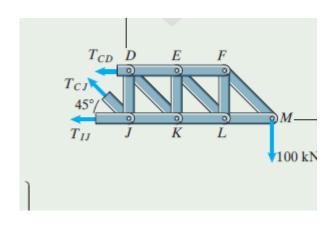


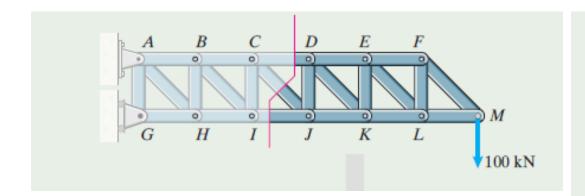




The horizontal members of the truss are each 1 m in length. Determine the axial forces in members CD, CJ, and IJ.

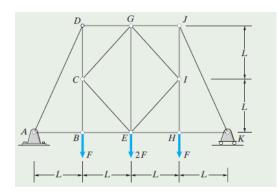


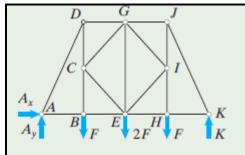




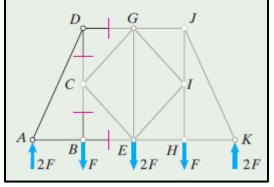
$$\begin{split} \Sigma F_x &= -T_{CD} - T_{CJ} \cos 45^\circ - T_{IJ} = 0, \\ \Sigma F_y &= T_{CJ} \sin 45^\circ - 100 \text{ kN} = 0, \\ \Sigma M_{\text{point }J} &= (1 \text{ m}) T_{CD} - (3 \text{ m}) (100 \text{ kN}) = 0. \\ \text{Solving yields } T_{CD} &= 300 \text{ kN}, T_{CJ} = 141 \text{ kN}, \\ \text{and } T_{IJ} &= -400 \text{ kN}. \text{ The axial loads are} \\ CD: 300 \text{ kN (T), } CJ: 141 \text{ kN (T),} \\ IJ: 400 \text{ kN (C).} \end{split}$$

Determine the axial forces in members DG and BE of the truss.





(a) Free-body diagram of the entire truss.

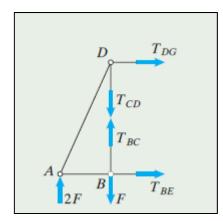


$$\Sigma F_x = A_x = 0,$$

$$\Sigma F_y = A_y + K - F - 2F - F = 0,$$

$$\Sigma M_{\text{point }A} = -LF - (2L)(2F) - (3L)F + (4L)K = 0,$$

we obtain the reactions $A_x = 0$, $A_y = 2F$, and K = 2F.



$$\Sigma M_{\text{point }B} = -L(2F) - (2L)T_{DG} = 0.$$

The axial force $T_{DG} = -F$. Then, from the equilibrium equation

$$\Sigma F_x = T_{DG} + T_{BE} = 0,$$

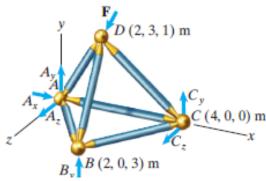
we see that $T_{BE} = -T_{DG} = F$. Member DG is in compression, and member BE is in tension.

Reticulados Espaciales









$$A_{x}$$

$$A_{z}$$

$$B_{y}$$

$$B (2, 0, 3) \text{ m}$$

$$D$$

$$A \text{ k N}$$

$$\Sigma F_{x} = A_{x} - 2 = 0,$$

$$\Sigma F_{y} = A_{y} + B_{y} + C_{y} - 6 = 0,$$

$$\Sigma F_{z} = A_{z} + C_{z} - 1 = 0,$$

$$\Sigma M_{\text{point } A} = (\mathbf{r}_{AB} \times B_{y} \mathbf{j}) + [\mathbf{r}_{AC} \times (C_{y} \mathbf{j} + C_{z} \mathbf{k})] + (\mathbf{r}_{AD} \times \mathbf{F})$$

$$= \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 2 & 0 & 3 \\ 0 & B_{y} & 0 \end{vmatrix} + \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 4 & 0 & 0 \\ 0 & C_{y} & C_{z} \end{vmatrix} + \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 2 & 3 & 1 \\ -2 & -6 & -1 \end{vmatrix}$$

$$= (-3B_{y} + 3)\mathbf{i} + (-4C_{z})\mathbf{j}$$

$$+ (2B_{y} + 4C_{y} - 6)\mathbf{k} = 0.$$

$$\mathbf{r}_{CB} = (2 - 4)\mathbf{i} + (0 - 0)\mathbf{j} + (3 - 0)\mathbf{k} = -2\mathbf{i} + 3\mathbf{k} (\mathbf{m}).$$
 $\mathbf{e}_{CB} = \frac{\mathbf{r}_{CB}}{|\mathbf{r}_{CB}|} = -0.555\mathbf{i} + 0.832\mathbf{k},$

$$T_{BC} \mathbf{e}_{CB} = T_{BC}(-0.555\mathbf{i} + 0.832\mathbf{k}).$$
 $T_{CD}(-0.535\mathbf{i} + 0.802\mathbf{j} + 0.267\mathbf{k}).$

$$T_{CD}$$
 $C_y = 1 \text{ kM}$
 T_{BC}
 C

1 kN

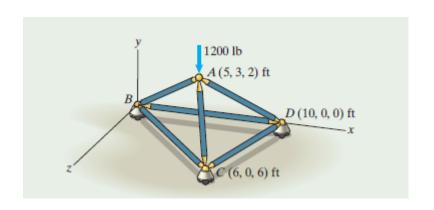
2kN 1 kN

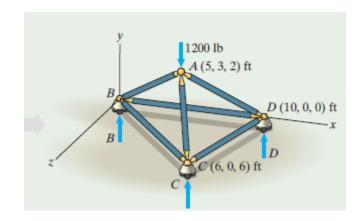
$$-T_{AC}\mathbf{i} + T_{BC}(-0.555\mathbf{i} + 0.832\mathbf{k}) + T_{CD}(-0.535\mathbf{i} + 0.802\mathbf{j} + 0.267\mathbf{k}) + (1 \text{ kN})\mathbf{j} = 0,$$

$$\Sigma F_x = -T_{AC} - 0.555T_{BC} - 0.535T_{CD} = 0,$$

 $\Sigma F_y = 0.802T_{CD} + 1 \text{ kN} = 0,$
 $\Sigma F_z = 0.832T_{BC} + 0.267T_{CD} = 0.$

Calcular los esfuerzos en AD, BD, y CD



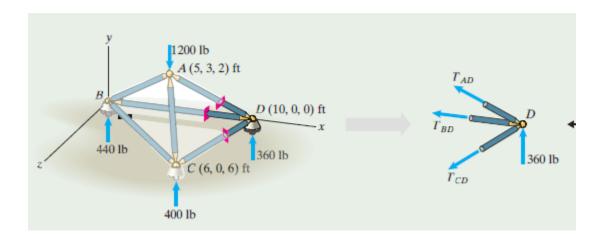


$$\Sigma F_{y} = B + C + D - 1200 \text{ lb} = 0,$$

$$\Sigma M_{\text{point } B} = \mathbf{r}_{BA} \times [-1200 \mathbf{j} (\text{lb})] + \mathbf{r}_{BC} \times C \mathbf{j} + \mathbf{r}_{BD} \times D \mathbf{j}$$

$$= \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 5 & 3 & 2 \\ 0 & -1200 & 0 \end{vmatrix} + \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 6 & 0 & 6 \\ 0 & C & 0 \end{vmatrix} + \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 10 & 0 & 0 \\ 0 & D & 0 \end{vmatrix}$$

$$= (2400 - 6C)\mathbf{i} + (-6000 + 6C + 10D)\mathbf{k} = 0.$$
Solving yields $B = 440$ lb, $C = 400$ lb, and $D = 360$ lb.



$$\mathbf{r}_{DA} = -5\mathbf{i} + 3\mathbf{j} + 2\mathbf{k} \text{ (ft)}.$$

$$\mathbf{e}_{DA} = \frac{\mathbf{r}_{DA}}{|\mathbf{r}_{DA}|} = -0.811\mathbf{i} + 0.487\mathbf{j} + 0.324\mathbf{k}.$$

$$T_{AD}\mathbf{e}_{DA} = T_{AD}(-0.811\mathbf{i} + 0.487\mathbf{j} + 0.324\mathbf{k}),$$

$$T_{BD}\mathbf{e}_{DB} = -T_{BD}\mathbf{i},$$

$$T_{CD}\mathbf{e}_{DC} = T_{CD}(-0.555\mathbf{i} + 0.832\mathbf{k}).$$

$$T_{AD}\mathbf{e}_{DA} + T_{BD}\mathbf{e}_{DB} + T_{CD}\mathbf{e}_{DC} + (360 \text{ lb})\mathbf{j} = 0.$$

The i, j, and k components of this equation must each equal zero, resulting in the three equations

$$-0.811T_{AD} - T_{BD} - 0.555T_{CD} = 0,$$

$$0.487T_{AD} + 360 \text{ lb} = 0,$$

$$0.324T_{AD} + 0.832T_{CD} = 0.$$

Solving yields $T_{AD} = -740$ lb, $T_{BD} = 440$ lb, and $T_{CD} = 288$ lb. The axial forces are AD: 740 lb (C), BD: 440 lb (T), CD: 288 lb (T).

Problem 6.66 The free-body diagram of the part of the construction crane to the left of the plane is shown. The coordinates (in meters) of the joints A, B, and C are (1.5, 1.5, 0), (0, 0, 1), and (0, 0, -1), respectively. The axial forces P_1 , P_2 , and P_3 are parallel to the x axis. The axial forces P_4 , P_5 , and P_6 point in the directions of the unit vectors

$$e_4 = 0.640i - 0.640j - 0.426k$$

$$e_5 = 0.640i - 0.640j - 0.426k,$$

$$e_6 = 0.832i - 0.555k$$

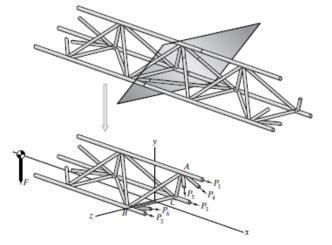
The total force exerted on the free-body diagram by the weight of the crane and the load it supports is $-F\mathbf{j} = -44\mathbf{j}$ (kN) acting at the point (-20, 0, 0) m. What is the axial force P_3 ?

Strategy: Use the fact that the moment about the line that passes through joints A and B equals zero.

 $\mathbf{M}_{B} = \begin{bmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ -20 & 0 & -1 \\ 0 & -44 & 0 \end{bmatrix} + \begin{bmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 0 & -2 \\ P_{3} & 0 & 0 \end{bmatrix}$

 $= -44i - 2P_3j + 880k$ (kN-m).





The position vector from B to A is

$$\mathbf{r}_{BA} = 1.5\mathbf{i} + 1.5\mathbf{j} - \mathbf{k} \ (\mathbf{m}),$$

and the unit vector that points from B toward A is

$$e_{\text{BA}} = \frac{\mathbf{r}_{\text{BA}}}{|\mathbf{r}_{\text{BA}}|} = 0.640\mathbf{i} + 0.640\mathbf{j} - 0.426\mathbf{k}.$$

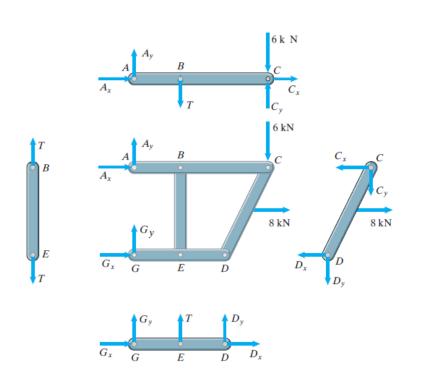
From the condition that

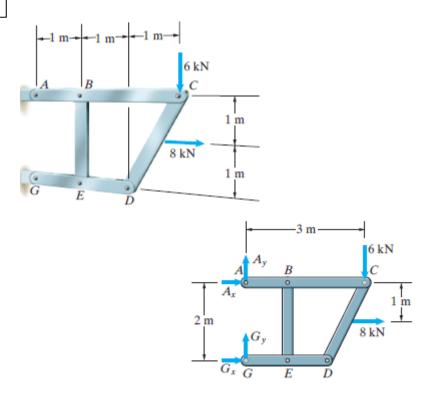
$$\mathbf{e}_{BA} \cdot \mathbf{M}_B = 0.640(-44) + 0.640(-2P_3)$$

- $0.426(880) = 0$,

we obtain
$$P_3 = -315$$
 kN.

Bastidores y Marcos





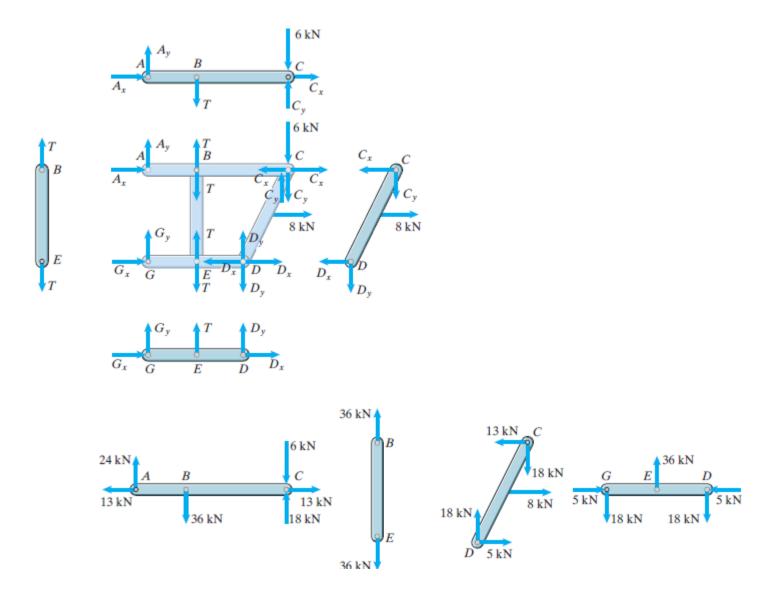
$$\Sigma M_{\text{point }A} = (2 \text{ m})G_x + (1 \text{ m})(8 \text{ kN}) - (3 \text{ m})(6 \text{ kN}) = 0,$$

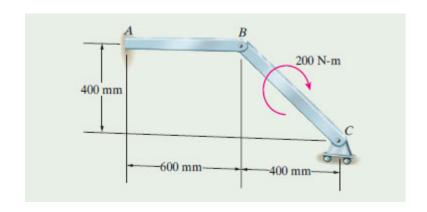
and we obtain the reaction $G_x = 5$ kN. Then, from the equilibrium equation

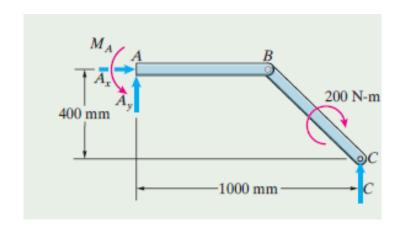
$$\Sigma F_x = A_x + G_x + 8 \text{ kN} = 0,$$

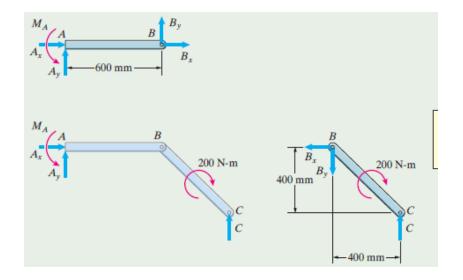
we obtain the reaction $A_x = -13$ kN. Although we cannot determine A_y or G_y from the free-body diagram of the entire structure, we can do so by analyzing the individual members.

Tengo Ax= -13 y Gx=5



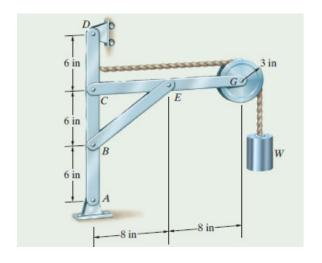


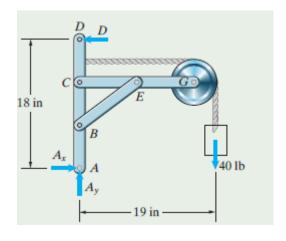


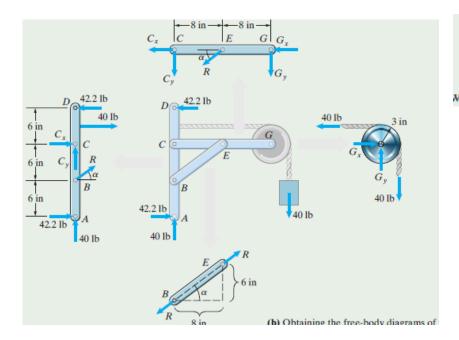


$$\Sigma F_x = A_x = 0,$$

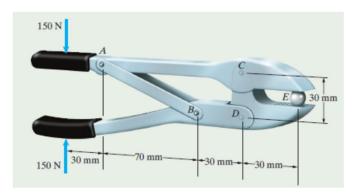
 $\Sigma F_y = A_y + C = 0,$
 $\Sigma M_{\text{point } A} = M_A - 200 \text{ N-m} + (1.0 \text{ m})C = 0.$

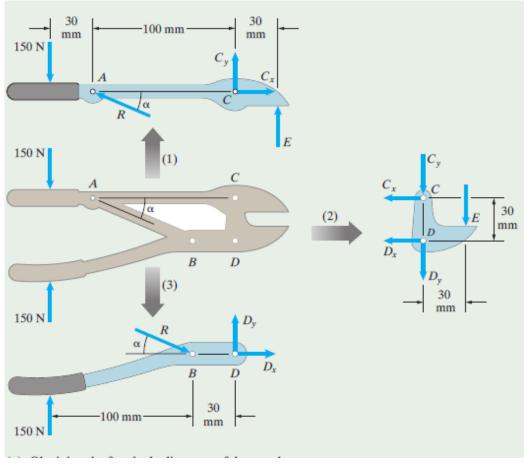




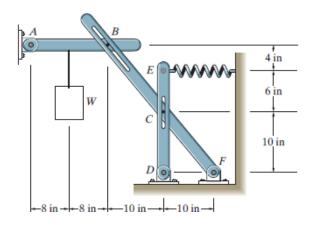


$$\Sigma F_x = A_x - D = 0,$$
 $\Sigma F_y = A_y - 40 \text{ lb} = 0,$
 $\Sigma M_{\text{point } A} = (18 \text{ in}) D - (19 \text{ in}) (40 \text{ lb}) = 0,$
we obtain the reactions $A_x = 42.2 \text{ lb}, A_y = 40 \text{ lb}, \text{ and } D = 42.2 \text{ lb}.$



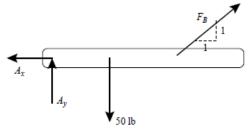


Calcule la fuerza en el Resorte



$$\sum M_A : -(50 \text{ lb})(8 \text{ in}) + \frac{1}{\sqrt{2}} F_B(16 \text{ in}) = 0 \Rightarrow F_B = 35.4 \text{ lb}$$

$$\sum M_D : -T(16 \text{ in}) + F_C(10 \text{ in}) = 0 \Rightarrow T = 62.5 \text{ lb}$$

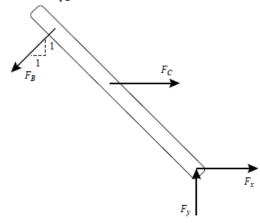


Now examine BCF

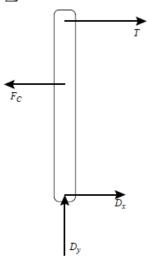
$$\sum M_F : F_B(20\sqrt{2}) \text{ in} - F_C(10 \text{ in}) = 0 \Rightarrow F_C = 100 \text{ lb}$$

$$\sum F_x : -\frac{1}{\sqrt{2}}F_B + F_C + F_x = 0 \Rightarrow F_x = -75 \text{ lb}$$

$$\sum F_y : -\frac{1}{\sqrt{2}}F_B + F_y = 0 \Rightarrow F_y = 25 \text{ lb}$$



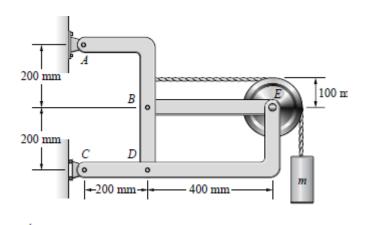
$$\sum M_D : -T(16 \text{ in}) + F_C(10 \text{ in}) = 0 \Rightarrow T = 62.5 \text{ lb}$$

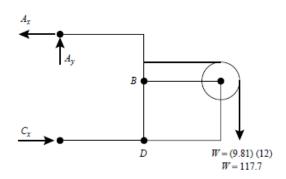


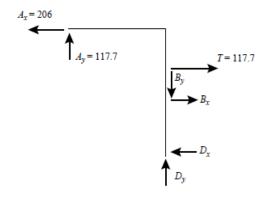
Summary

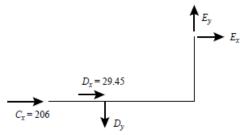
Tension in Spring = 62.5 lb

$$F_x = 25$$
 lb, $F_y = -75$ lb

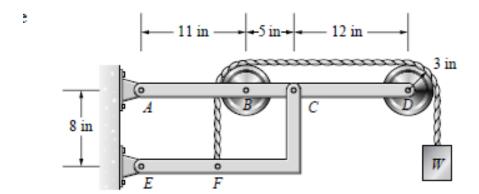


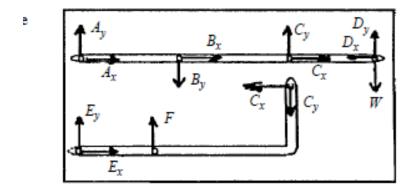






Resolver









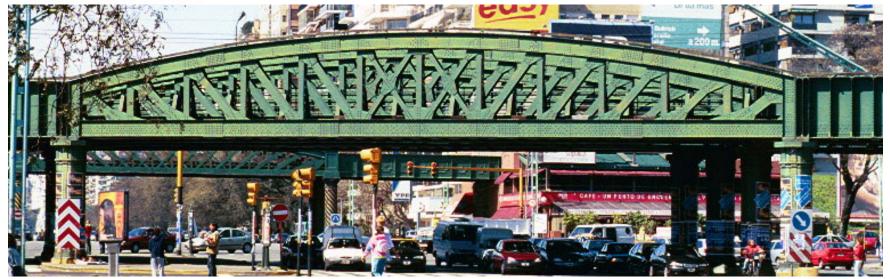






FACULTAD DE INGENIERIA

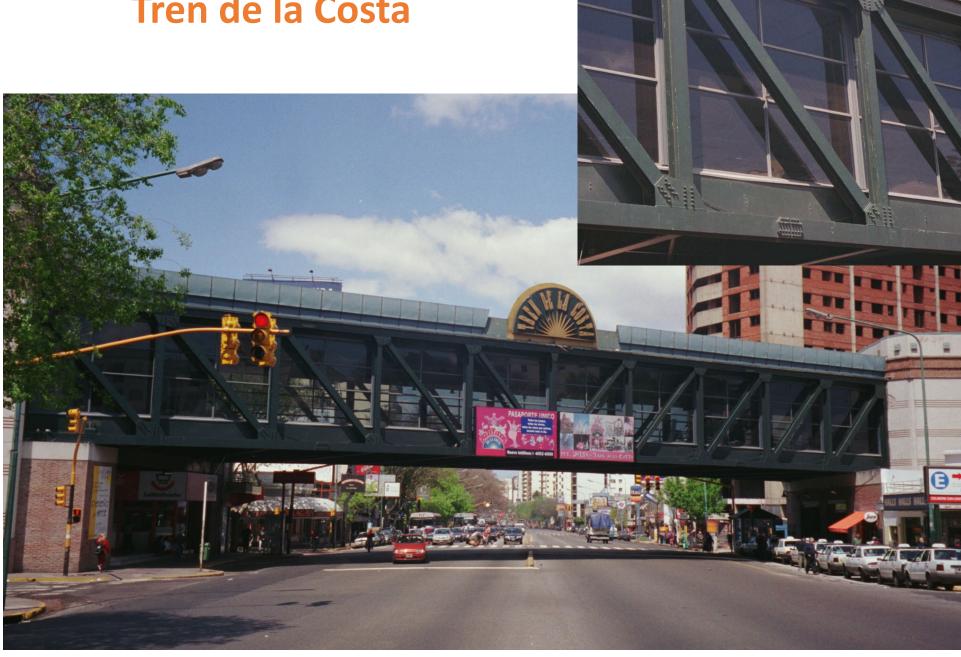


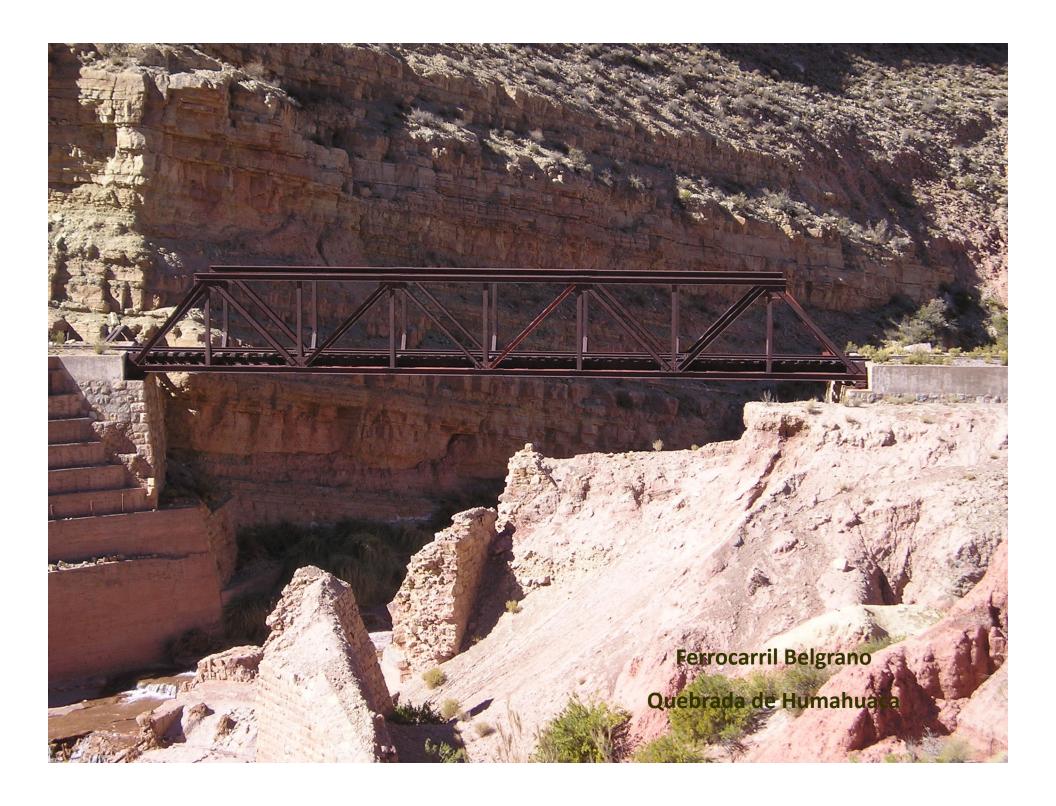






Tren de la Costa



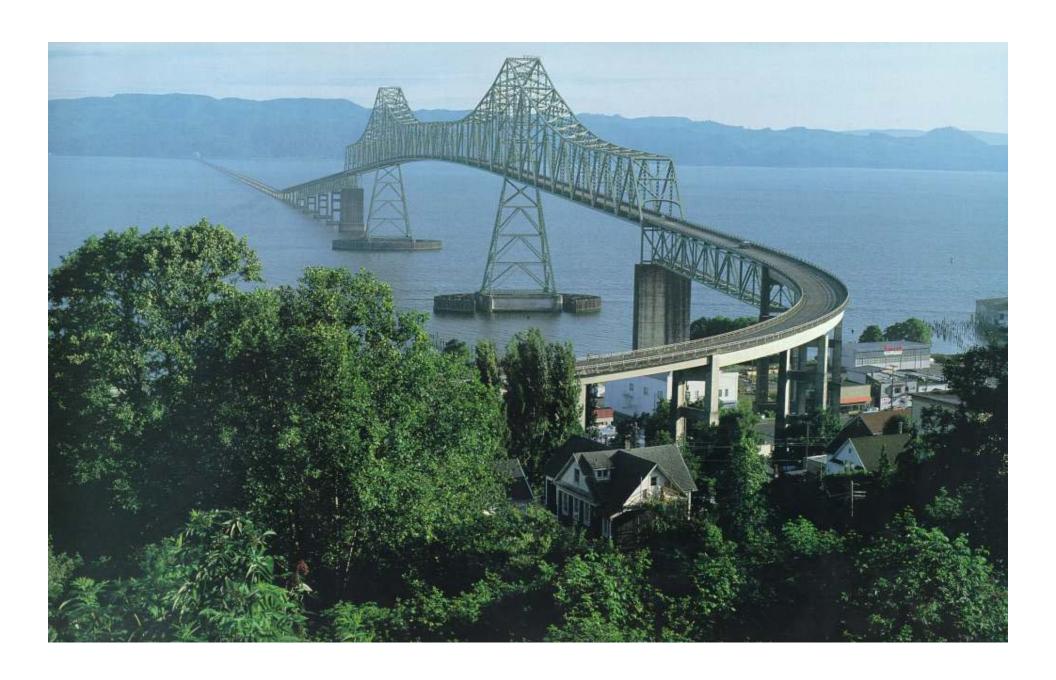


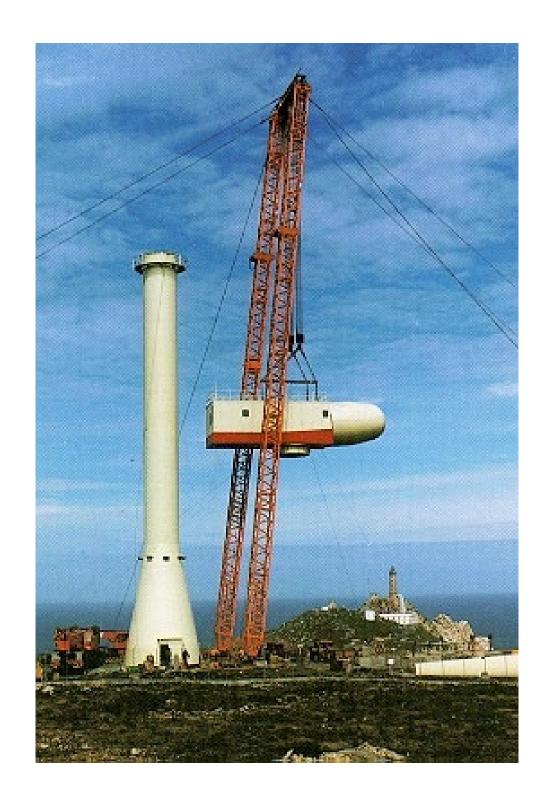


Tren a las Nubes Salta











Puentes Nicolás Avellaneda – Riachuelo – Buenos Aires





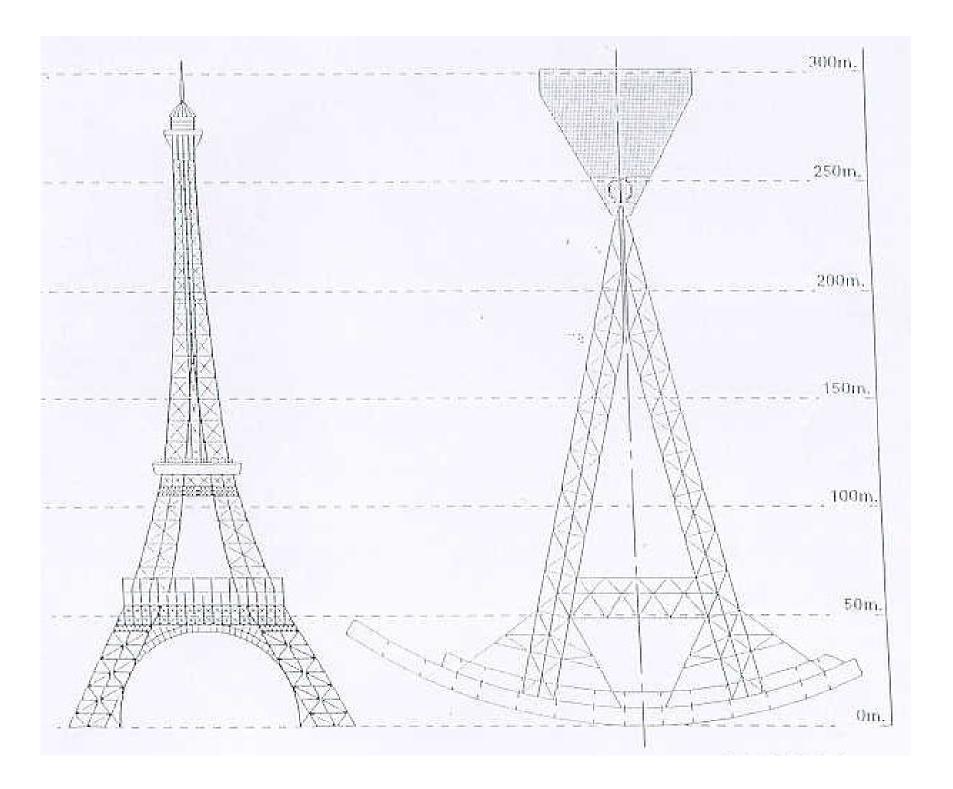
Puente levadizo basculante BARRACA PEÑA - 1913 Riachuelo – Buenos Aires

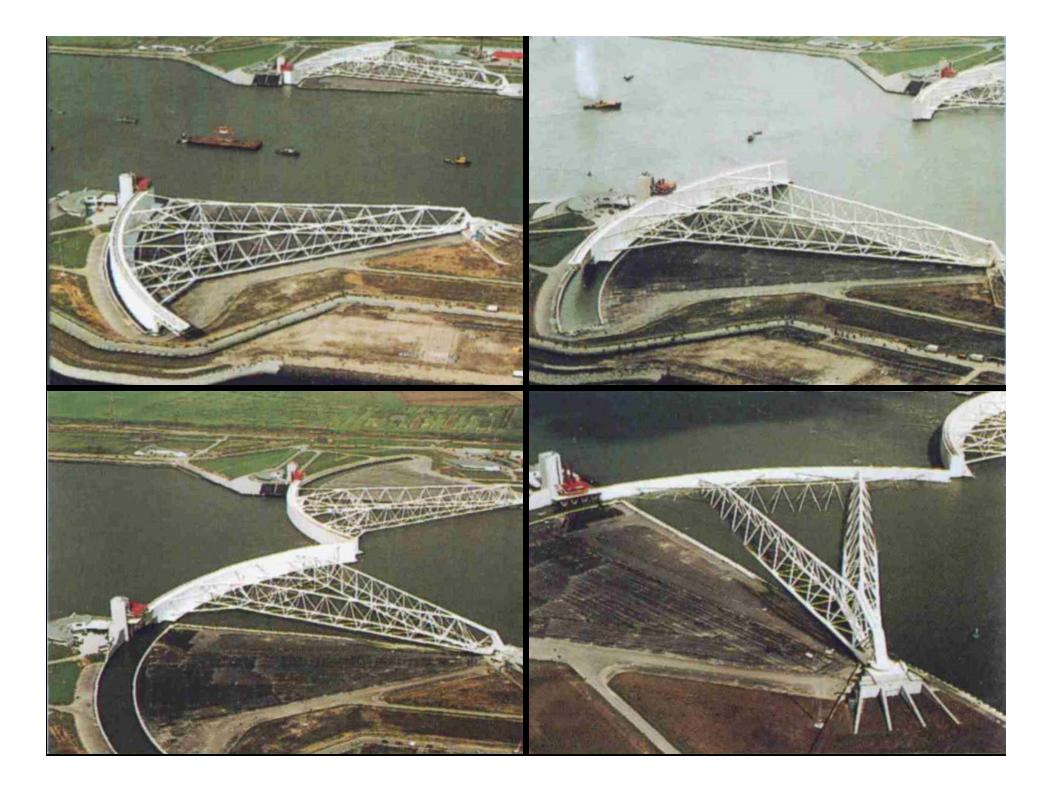




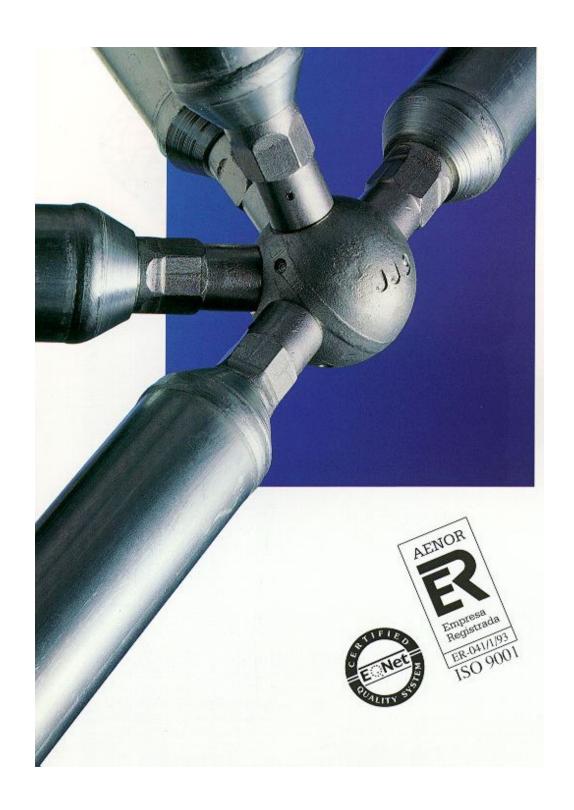


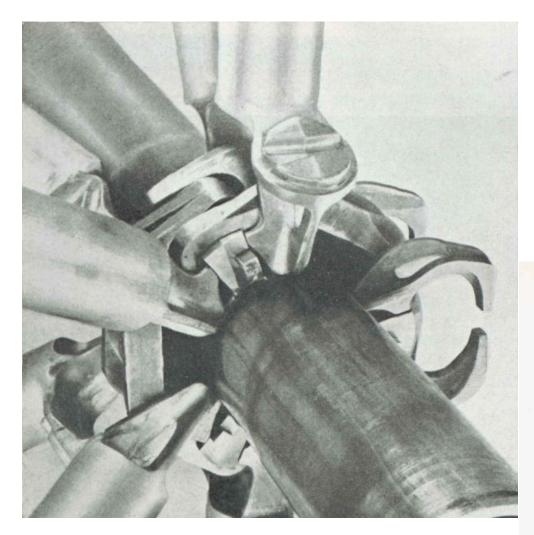
ENTRADA AL PUERTO DE ROTTERDAM











Sistema K. WACHSMANN

Sistema TRIODETIC

